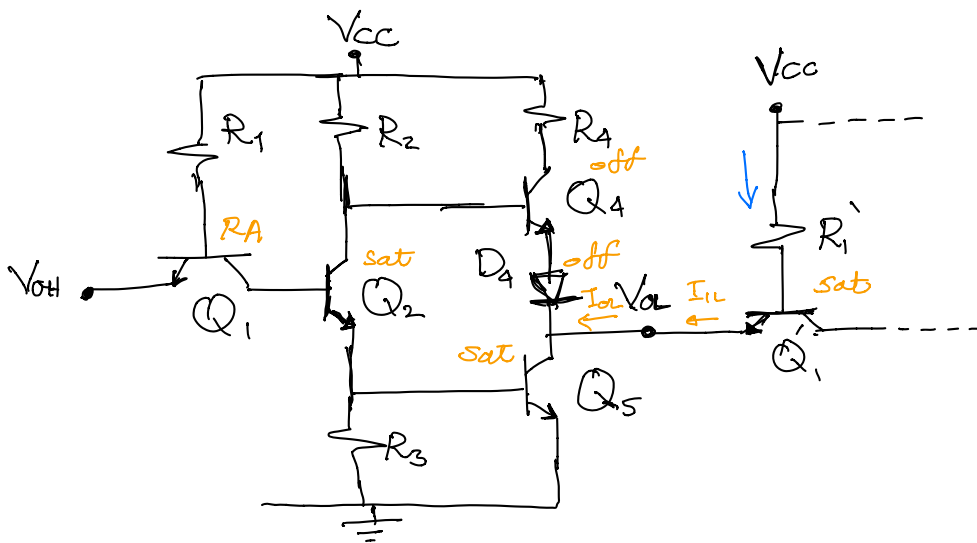


Question 2: [7 Marks]

For the standard TTL inverter shown in question 1, give values for all the resistors if:

$V_{OL} = 0.2V$, $V_{IL} = 0.5V$, $V_{IB} = 1.2V$, $V_{OB} = 6.6V$, $V_{IH} = 1.4V$, $V_{OH} = 8.6V$, $P(OH) = 10mW$, and $P(OL) = 35.8mW$



$$V_{OH} = V_{CC} - V_{BE(FA)} - V_D(ON)$$

$$V_{CC} = V_{OH} + V_{BE(FA)} + V_D(ON) = 8.6 + 2(0.7) = 10V$$

$$V_{CC} = 10V$$

$$V_{OL} = V_{CE(sat)} = 0.2V \Rightarrow V_{CE(sat)} = 0.2V$$

$$V_{IL} = V_{BE(FA)} - V_{CE(sat)}$$

$$V_{BE(FA)} = V_{IL} + V_{CE(sat)} = 0.5 + 0.2 = 0.7V$$

$$V_{BE(FA)} = 0.7V$$

$$V_{IH} = 2V_{BE(sat)} - V_{CE(sat)}$$

$$V_{BE(sat)} = \frac{V_{IH} + V_{CE(sat)}}{2} = \frac{1.4 + 0.2}{2} = 0.8V$$

$$V_{BE(sat)} = 0.8V$$

$$P_{(OH)} = I_{e(OH)} \times V_{CC} = I_{R1(OH)} \times V_{CC}$$

$$I_{R1(OH)} = \frac{P_{(OH)}}{V_{CC}} = \frac{10mW}{10} = 1mA$$

$$I_{R1(OH)} = \frac{V_{CC} - V_{BE(sat)} - V_{CE(sat)}}{R_1}$$

$$R_1 = \frac{5 - 0.8 - 0.2}{1m} = 4k\Omega \Rightarrow R_1 = 4k\Omega$$

Assume $\beta_f \gg 1$, neglect I_B 's

$$I_{R2(OL)} = I_{C2} = I_{E2} = I_{R3}$$

$$V_{OB} = V_{CC} - I_{R2(OL)} R_2 - V_{BE(FA)} - V_{D(ON)}$$

$$\text{but } I_{R3} = \frac{V_{BE(FA)}}{R_3}$$

$$V_{OB} = V_{CC} - \frac{R_2}{R_3} V_{BE(FA)} - V_{BE(FA)} - V_{D(ON)}$$

$$\frac{R_2}{R_3} = \frac{V_{CC} - V_{OB} - V_{BE(FA)} - V_{D(ON)}}{V_{BE(FA)}} = \frac{10 - 6.6 - 0.7 - 0.7}{0.7}$$

$$\frac{R_2}{R_3} = 2.857 \Rightarrow R_2 = 2.857 R_3$$

$$I_{R1(OL)} = \frac{V_{CC} - V_{BC(FA)} - 2V_{BE(sat)}}{R_1} = \frac{10 - 0.7 - 2(0.8)}{4k}$$

$$I_{R1(OL)} = 1.925mA$$

$$P_{(OL)} = [I_{R1(OL)} + I_{R2(OL)}] V_{CC}$$

$$I_{R1(OL)} + I_{R2(OL)} = 3.58mA$$

$$I_{R2}(OL) = 3.58 \text{ mA} - 1.925 \text{ mA} = 1.655 \text{ mA}$$

$$I_{R3} = \frac{V_{BE(sat)}}{R_3}$$

$$R_3 = \frac{V_{BE(sat)}}{I_{R3}} = \frac{0.8}{1.655 \text{ mA}} = 0.483 \text{ k}\Omega$$

$$R_3 = 0.483 \text{ k}\Omega$$

$$R_2 = 2.857 R_3 = 2.857 \times 0.483 \text{ k}\Omega = 1.38 \text{ k}\Omega$$

$$R_2 = 1.38 \text{ k}\Omega$$

Since R_4 is typically the tenth of R_2

$$R_4 = \frac{R_2}{10} = \frac{1.38 \text{ k}\Omega}{10}$$

$$R_4 = 138 \Omega$$

$$R_1 = 4 \text{ k}\Omega$$

$$R_2 = 1.38 \text{ k}\Omega$$

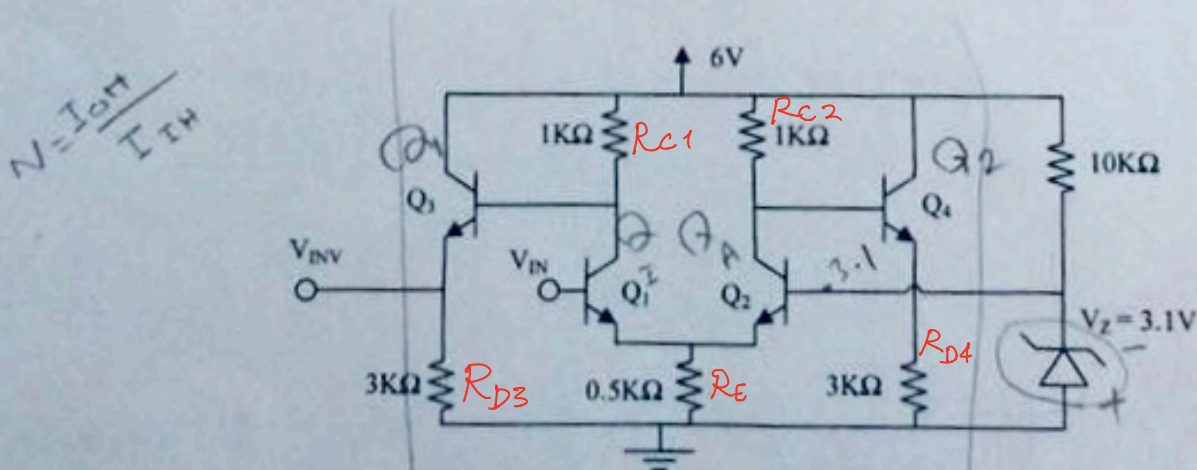
$$R_3 = 0.483 \text{ k}\Omega$$

$$R_4 = 138 \Omega$$

Question 3: [6 Marks]

For the ECL inverter shown in the following figure. Assume $\beta_F = 50$ and $V_{BE(ECL)} = 0.75 \text{ V}$.

- Sketch the VTC. Please calculate and label all voltages including V_S
- Determine the maximum fan-out of the inverter. Assume that the load gates have reduced V_{OH} of the driving gate by 25 mV .
- Calculate the average power dissipation of the inverter.



$$V_{BB} = V_E = 3.1V$$

V_{OH} :

for $V_{in} < V_E$ Q_1 is off

$$V_{OH} = V_{CC} - I_{B3}R_{C1} - V_{BE3}(ECL) = 6 - I_{B3} \times 1K - 0.75$$

$$V_{CC} - I_{B3}R_{C1} - V_{BE3}(ECL) - I_{E3}R_{D3} = 0$$

$$\text{But } I_E = (1 + \beta_f) I_B$$

$$V_{CC} - I_{B3}R_{C1} - V_{BE3}(ECL) - (1 + \beta_f) I_{B3}R_{D3} = 0$$

$$I_{B3} = \frac{V_{CC} - V_{BE3}(ECL)}{R_{C1} + (1 + \beta_f)R_{D3}} = \frac{6 - 0.75}{1K + (1 + 50)3K} = 34.1 \mu A$$

$$V_{OH} = 6 - 0.0341m \times 1K - 0.75 = 5.22V$$

$$\boxed{V_{OH} = 5.22V}$$

V_{IL} & V_{IH} :

$$V_{IL} = V_{BB} - 0.05 = 3.1 - 0.05 = 3.05V$$

$$V_{IH} = V_{BB} + 0.05 = 3.1 + 0.05 = 3.15V$$

$$\boxed{V_{IL} = 3.05V}$$

$$\boxed{V_{IH} = 3.15V}$$

V_{OL} : for $V_{in} > V_E$ Q_1 is FA

$$V_{OL} = V_{CC} - I_{C1}R_{C1} - V_{BE3}(ECL) = 6 - I_{C1} \times 1K - 0.75$$

$$I_{C1} \approx I_{E1} = \frac{V_{in} - V_{BE1}(ECL)}{R_E} \quad , \text{ but } V_{in} = V_{IH}$$

$$= \frac{3.15 - 0.75}{0.5K} = 4.8mA$$

$$V_{OL} = 6 - 4.8m \times 1K - 0.75 = 0.45V$$

$$\boxed{V_{OL} = 0.45V}$$

V_S :

when V_{IN} increases beyond V_{IH} Q_1 saturate @
 $V_{IN} = V_S$

$$I_{C1} \approx I_{E1} = \frac{V_{IN} - V_{BE1}(sat)}{R_E}$$

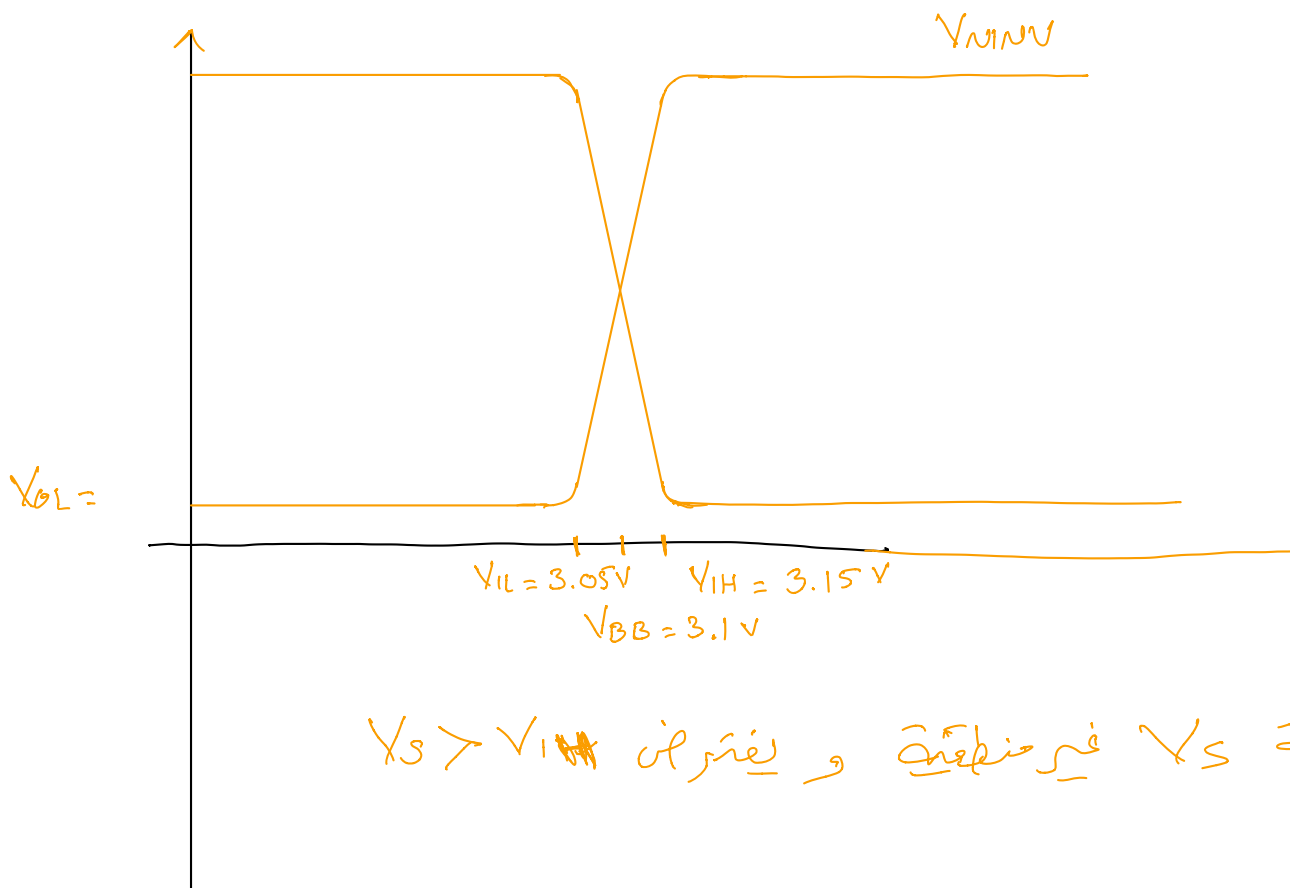
$$V_{INV} = V_{CC} - I_{C1} R_{C1} - V_{BE3}(ECL) \quad \text{--- (1)}$$

$$V_{INV} = V_{IN} - V_{BC1}(sat) - V_{BE3}(ECL) \quad \text{--- (2)}$$

Solve (1) & (2) for ($V_{IN} = V_S$)

$$V_S = \frac{V_{CC} + \frac{R_{C1}}{R_E} V_{BE1}(sat) + V_{BC1}(sat)}{1 + \frac{R_{C1}}{R_E}}$$
$$= \frac{6 + \left(\frac{1K}{0.5K}\right)(0.8) + 0.6}{1 + \frac{1K}{0.5K}} = \frac{6 + 2 \times 0.8 + 0.6}{1 + 2} = 2.73 V$$

$V_S = 2.73 V$



$V_S > V_{IH}$ \Rightarrow Q_1 is in saturation & Q_2 is in cutoff